2015-DSE MATH EP M1

> HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2015

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8.30 am - 11.00 am (2% hours)This paper must be answered in English

INSTRUCTIONS

- 1. After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- 2. This paper consists of TWO sections, A and B.
- 3. Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- 4. Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- 5. Unless otherwise specified, all working must be clearly shown.
- 6. Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- 7. No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

Candidate Number

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2015-DSE-MATH-EP(M1)-1

4

SECTION A (50 marks)

1.

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The table below shows the probability distribution of a discrete random variable X, where a and b are constants:

x	2	3	5	7	9
$\mathbf{P}(X=x)$	0.08	0.15	а	0.45	b

It is given that E(X) = 5.64. Find

(a) a and b,

(b) $E((6-5X)^2)$ and Var(6-5X).

(6 marks)

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(a) Find $P(A' \cap B')$ and	$\mathbb{P}(A' \cap B)$.		
(b) Are A and B mutually	ly exclusive? Explain your answ	wer.	(6 mar

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If a Final interv	yellow ly, the i viewee i	ball is drawn, then the interviewee considers the question 'Are you a non-smoker?' interviewee answers either 'Yes' or 'No'. Let p be the probability that a randomly selected is a smoker.
(a)	Expre	ess, in terms of p , the probability that a randomly selected interviewee answers 'Yes'.
(b)	In thi	s survey, 50 out of 91 interviewees answer 'Yes'.
	(i)	Find p .
	(ii)	Given that an interviewee answers 'No', find the probability that the interviewee is non-smoker. (6 mark
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4.	A ma packe the re John	nufacturer of brand B biscuits starts a promotion plan by giving one reward points card in each t of biscuits. It is found that 75% of the packets of brand B biscuits contain 3-point cards and est contain 7-point cards. A total of 20 points or more can be exchanged for a gift coupon. buys 4 packets of brand B biscuits and he opens them one by one.
	(a)	Find the probability that John gets the first 7-point card when the 4th packet of brand B biscuits has been opened.
	(b)	Find the probability that John can exchange for a gift coupon.
	(c)	Given that John can exchange for a gift coupon, find the probability that he gets a 7-point card when the 4th packet of brand B biscuits has been opened.
		(7 marks)

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(a)	Expand e^{-4x} in ascending powers of x as far as the term in x^2 .	
(b)	Find the coefficient of x^2 in the expansion of $\frac{(2+x)^5}{e^{4x}}$.	(5
		(5 marks)
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(a)	Find the x-coordinates of the two points of intersection of C_1 and C_2 .	
(b)	Express, in terms of e , the area of the region bounded by C_1 and C_2 .	(6 mark
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Cons	ider the curve $C: y = x\sqrt{2x^2 + 1}$.
(a)	Find $\frac{dy}{dx}$.
(b)	Two of the tangents to C are perpendicular to the straight line $3x + 17y = 0$. Find the equations
	of the two tangents. (7 marks)
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(a)	Express $\frac{d}{dx}(x^6+1)\ln(x^2+1))$ in the form $f(x)+g(x)\ln(x^2+1)$, where $f(x)$ and $g(x)$ are polynomials.
(b)	Find $\int x^5 \ln(x^2 + 1) dx$. (7 marks)
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SECTION B (50 marks)

- 9. The speeds of cars passing a checkpoint on a highway follow a normal distribution with a mean of μ km/h and a standard deviation of 16 km/h.
 - (a) A survey on the speeds of cars to estimate μ is conducted.
 - (i) A random sample of 25 cars is taken and the stem-and-leaf diagram below shows the distribution of their speeds (in km/h) :

Stem (tens) Leaf (units) 6 0 2 3 7 0 1 2 5 5 6 6 1 1 7 2 5 5 6 1 1 3 8 3 7 6

Find a 95% confidence interval for μ .

(ii) Find the least sample size to be taken such that the width of a 97.5% confidence interval for μ is less than 9.

(7 marks)

- (b) Suppose that $\mu = 66$. If the speed of a car passing the checkpoint exceeds 90 km/h, a penalty ticket will be issued.
 - (i) If a car passes the checkpoint, find the probability that a penalty ticket will be issued.
 - (ii) If 12 cars pass the checkpoint, find the probability that more than 2 penalty tickets will be issued.

(5 marks)

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10. The number of customers buying tickets at cinema A in a minute can be modelled by a Poisson distribution with a mean of 3.2. The probability distribution of the number of tickets bought by a customer at cinema A is shown in the following table:

Number of tickets bought	1	2	3	4	5	6	≥ 7
Probability	0.12	0.7	0.08	0.04	0.03	0.02	0.01

Find the probability that fewer than 4 customers buy tickets at cinema A in a certain minute. (a) (3 marks)

- (b) Find the probability that the 8th customer buying tickets at cinema A is the 3rd customer who buys 2 tickets. (2 marks)
- (c) Find the probability that exactly 3 customers buy tickets at cinema A in a certain minute and each of them buys 2 tickets. (2 marks)
- (d) Find the probability that exactly 3 customers buy tickets at cinema A in a certain minute and they buy a total of 6 tickets. (3 marks)
- Given that fewer than 4 customers buy tickets at cinema A in a certain minute, find the (e) probability that they buy a total of 6 tickets. (3 marks)

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11. An engineer models the rates of change of the amount of oil produced (in hundred barrels per day) by oil companies X and Y respectively by

$$f(t) = \ln(e^t - t)$$
 and $g(t) = \frac{8t}{1+t}$,

where $t (2 \le t \le 12)$ is the time measured in days.

- (a) Using the trapezoidal rule with 5 sub-intervals, estimate the total amount of oil produced by oil company X from t = 2 to t = 12. (3 marks)
- (b) Determine whether the estimate in (a) is an over-estimate or an under-estimate. Explain your answer. (3 marks)
- (c) Find $\int \frac{t}{1+t} dt$.
- (d) The engineer claims that the total amount of oil produced by oil company X from t = 2 to t = 12 is less than that of oil company Y. Do you agree? Explain your answer. (3 marks)

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12. In an experiment, the temperature (in °C) of a certain liquid can be modelled by $S = \frac{200}{1+a2^{bt}} ,$ where a and b are constants and t is the number of hours elapsed since the start of the experiment. Express $\ln\left(\frac{200}{S}-1\right)$ as a linear function of t. (a) (2 marks) (b) It is found that the intercepts on the vertical axis and the horizontal axis of the graph of the linear function obtained in (a) are ln 4 and 4 respectively. Find a and b. (i) Find $\frac{\mathrm{d}S}{\mathrm{d}t}$ and $\frac{\mathrm{d}^2S}{\mathrm{d}t^2}$. (ii) Describe how S and $\frac{dS}{dt}$ vary during the first 48 hours after the start of the Answers written in the margins will not be marked. (iii) experiment. Explain your answer. (11 marks)

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0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
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0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
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1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
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2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
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2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.



2015-DSE-MATH-EP(M1)-24

27