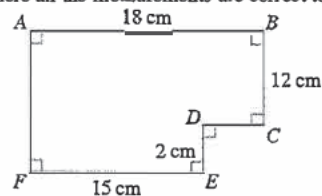


1 Estimation

1.1 HKCEE MA 2006 – I – 11

In the figure, $ABCDEF$ is a thin six-sided polygonal metal sheet, where all the measurements are correct to the nearest cm.



- Write down the maximum absolute error of the measurements.
- Find the least possible area of the metal sheet.
- The actual area of the metal sheet is $x \text{ cm}^2$. Find the range of values of x .

1.2 HKCEE MA 2007 I 10

- If the length of a piece of thin metal wire is measured as 5 cm correct to the nearest cm, find the least possible length of the metal wire.
- The length of a piece of thin metal wire is measured as 2.0 m correct to the nearest 0.1 m.
 - Is it possible that the actual length of this metal wire exceeds 206 cm? Explain your answer.
 - Is it possible to cut this metal wire into 46 pieces of shorter metal wires, with each length measured as 5 cm correct to the nearest cm? Explain your answer.

1.3 HKCEE MA 2008 – I – 7

John wants to buy the following items in a supermarket:

Item	Unit price	Quantity needed
Biscuit	\$8.2 per pack	4 packs
Chocolate	\$16.3 per box	3 boxes
Soft drink	\$4.8 per can	2 cans

- By rounding up the unit price of each item to the nearest dollar, estimate the total amount that John should pay.
- If John has only \$100, does he have enough money to buy all the items needed? Use the result of (a) to explain your answer.

1.4 HKCEE MA 2009 – I – 4

Round off 405.504 to

- the nearest integer,
- 2 decimal places,
- 2 significant figures.

1.5 HKCEE MA 2010 I 8

Three students, Peter, John and Henry have \$16.8, \$24.3 and \$32.5 respectively.

- By rounding down the amount owned by each student to the nearest dollar, estimate the total amount they have.
- If the three students want to buy a football of price \$70, will they have enough money to buy the football? Use the result of (a) to explain your answer.

1. ESTIMATION

1.6 HKCEE MA 2011 – I – 4

- Round off 8 091.1908 to the nearest ten.
- Round up 8 091.1908 to 3 significant figures.
- Round down 8 091.1908 to 3 decimal places.

1.7 HKDSE MA 2013 – I – 8

A pack of sea salt is termed *regular* if its weight is measured as 100 g correct to the nearest g.

- Find the least possible weight of a *regular* pack of sea salt.
- Is it possible that the total weight of 32 *regular* packs of sea salt is measured as 3.1 kg correct to the nearest 0.1 kg? Explain your answer.

1.8 HKDSE MA 2014 – I – 3

- Round up 123.45 to 1 significant figure.
- Round off 123.45 to the nearest integer.
- Round down 123.45 to 1 decimal place.

1.9 HKDSE MA 2017 – I – 9

A bottle is termed *standard* if its capacity is measured as 200 mL correct to the nearest 10 mL.

- Find the least possible capacity of a *standard* bottle.
- Someone claims that the total capacity of 120 *standard* bottles can be measured as 23.3 L correct to the nearest 0.1 L. Do you agree? Explain your answer.

1.10 HKDSE MA 2018 – I – 3

- Round up 265.473 to the nearest integer.
- Round down 265.473 to 1 decimal place.
- Round off 265.473 to 2 significant figures.

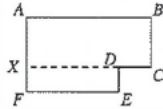
1.11 HKDSE MA 2020 – I – 3

- Round up 534.7698 to the nearest hundred.
- Round down 534.7698 to 2 decimal places.
- Round off 534.7698 to 2 significant figures.

1 Estimation

1.1 HKCEE MA 2006-I-11

- (a) Maximum absolute error = $1 \text{ cm} \div 2 = 0.5 \text{ cm}$
 (b) Least possible area of $ABCX = 17.5 \times 11.5 = 201.25 \text{ cm}^2$
 Least possible area of $DEFX = 1.5 \times 15.5 = 23.25 \text{ cm}^2$
 \therefore Least possible area of sheet = 224.5 cm^2
 (c) Upper limit of area = $18.5 \times 12.5 + 2.5 \times 16.5 = 272.5 \text{ cm}^2$
 $\therefore 224.5 \leq x < 272.5$



1.2 HKCEE MA 2007-I-10

- (a) Least possible length = $5 - 1 \div 2 = 4.5 \text{ (cm)}$
 (b) (i) Upper limit = $(2.0 + 0.1 \div 2) \text{ m} = 205 \text{ cm} < 206 \text{ cm}$
 \therefore No.
 (ii) Method 1
 Least possible total length of short wires
 $4.5 \text{ cm} \times 46 = 207 \text{ cm} > 205 \text{ cm}$
 \therefore No.
Method 2
 Upper limit of length of one short wire
 $= 205 \text{ cm} \div 46 = 4.4565 \text{ cm} < 4.5 \text{ cm}$
 \therefore No.

1.3 HKCEE MA 2008-I-7

- (a) Total amount $\approx \$ (9 \times 4 + 17 \times 3 + 5 \times 2) = \97
 (b) \therefore Actual amount $<$ Estimated amount $<$ \$100
 \therefore Yes.

1.4 HKCEE MA 2009-I-4

- (a) 406
 (b) 405.50
 (c) 410

1.5 HKCEE MA 2010-I-8

- (a) Total amount $\approx \$ (16 + 24 + 32) = \72
 (b) \therefore Actual amount $>$ Estimated amount $>$ \$70
 Yes.

1.6 HKCEE MA 2011-I-4

- (a) 8090
 (b) 8100
 (c) 8091.190

1.7 HKDSE MA 2013-I-8

- (a) Least possible weight = $(100 - 1 \div 2) \text{ g} = 99.5 \text{ g}$
 (b) Method 1
 Least possible total weight = $99.5 \text{ g} \times 32$
 $= 3184 \text{ g} = 3.2 \text{ kg}$, nearest 0.1 kg
 \therefore No.

Method 2

$$\text{Upper limit of weight of 1 pack} = \frac{3.1 + 0.1 \div 2}{32} \text{ kg}$$

$$= 98.43 \text{ g} < 99.5 \text{ g}$$

\therefore No.

1.8 HKDSE MA 2014-I-3

- (a) 100
 (b) 123
 (c) 123.4

1.9 HKDSE MA 2017-I-9

- (a) Least possible capacity = $(200 - 10 \div 5) \text{ mL} = 195 \text{ mL}$

Method 1

$$\text{Least total capacity} = 195 \text{ mL} \times 120 = 23.4 \text{ L} > 23.35 \text{ L}$$

\therefore No.

Method 2

$$\text{Upper limit of capacity of 1 bottle} = \frac{23.3 + 0.1 \div 2}{120} \text{ L}$$

$$= 194.58 \text{ mL} < 195 \text{ mL}$$

\therefore No.

1.10 HKDSE MA 2018-I-3

- (a) 266
 (b) 265.4
 (c) 270

1.11 HKDSE MA 2020-I-3

- | | |
|----|--------|
| 3a | 600 |
| b | 534.76 |
| c | 530 |