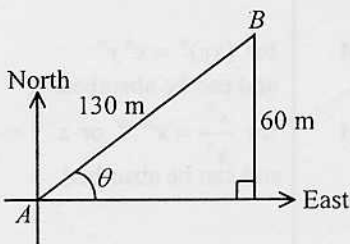
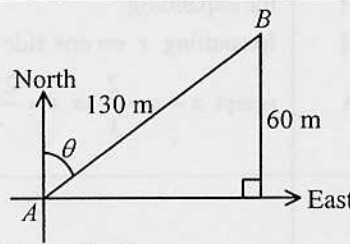


Solution	Marks	Remarks
<p>1. $\frac{(a^{-1}b)^3}{b^2} = \frac{a^{-3}b^3}{b^2}$</p> $= a^{-3}b$ $= \frac{b}{a^3}$	<p>1M</p> <p>1M</p> <p>1A</p> <p>------(3)</p>	<p>for $(xy)^n = x^n y^n$ and can be absorbed</p> <p>for $\frac{x^m}{x^n} = x^{m-n}$ or $x^{-n} = \frac{1}{x^n}$ and can be absorbed</p>
<p>2. $y = \frac{2}{a-x}$</p> $y(a-x) = 2$ $ay - xy = 2$ $-xy = 2 - ay$ $x = \frac{ay-2}{y}$	<p>1M</p> <p>1M</p> <p>1A</p>	<p>for expanding</p> <p>for putting x on one side</p> <p>accept $x = a - \frac{2}{y}$ or $x = \frac{2-ay}{-y}$</p>
$y = \frac{2}{a-x}$ $y(a-x) = 2$ $a-x = \frac{2}{y}$ $-x = \frac{2}{y} - a$ $x = a - \frac{2}{y}$	<p>1M</p> <p>1M</p> <p>1A</p> <p>------(3)</p>	<p>for making $a-x$ the subject</p> <p>for putting x on one side</p> <p>accept $x = \frac{ay-2}{y}$ or $x = \frac{2-ay}{-y}$</p>
<p>3. The amount</p> $= \$ 5000 (1+2\%)^3$ <p>The required interest</p> $= 5000 (1+2\%)^3 - 5000$ $= 306.04$ $\approx \$ 306$	<p>1A</p> <p>1M</p> <p>1A</p> <p>------(3)</p>	<p>u-1 for missing unit r.t. \$ 5 306</p> <p>for $5000 (1+r\%)^n - 5000 (n \geq 2)$</p> <p>u-1 for missing unit</p>
<p>4. Since $(a, 0)$ lies on $y = -x^2 + 10x - 25$, we have</p> $-a^2 + 10a - 25 = 0$ $-(a-5)^2 = 0$ $a = 5$ $b = -25$	<p>1M</p> <p>1A</p> <p>1A</p> <p>------(3)</p>	<p>for putting $y = 0$</p>

Solution	Marks	Remarks
<p>5.</p>  <p>Refer to the figure,</p> $\sin \theta = \frac{60}{130}$ $\theta \approx 27.48642625^\circ$ $\theta \approx 27.5^\circ$ <p>Thus, the bearing of B from A is N62.5°E.</p>	<p>1M</p> <p>1A</p> <p>1M</p>	<p>pp-1 for any undefined symbol</p> <p>u-1 for missing unit r.t. 27.5°</p> <p>accept 063 , 062.5° or N62°31'E</p>
 <p>Refer to the figure,</p> $\cos \theta = \frac{60}{130}$ $\theta \approx 62.51357375^\circ$ $\theta \approx 62.5^\circ$ <p>Thus, the bearing of B from A is N62.5°E.</p>	<p>1M</p> <p>1A</p> <p>1M</p>	<p>pp-1 for any undefined symbol</p> <p>u-1 for missing unit r.t. 27.5°</p> <p>accept 063 , 062.5° or N62°31'E</p>
<p>6. (a) $a^2 - ab + 2a - 2b$ $= a(a-b) + 2(a-b)$ $= (a+2)(a-b)$</p> <p>(b) $169y^2 - 25$ $= (13y)^2 - 5^2$ $= (13y+5)(13y-5)$</p>	<p>------(3)</p> <p>1M</p> <p>1A</p> <p>1M+1A</p> <p>------(4)</p> <p>1A</p> <p>1M+1A</p> <p>1A</p>	<p>for taking out a common factor or using cross-method</p> <p>pp-1 for any undefined symbol</p> <p>1M for $2x + 3(20 - x)$</p>
<p>7. Let the number of oranges bought be x. Then, the number of apples bought will be $20 - x$. Now, $2x + 3(20 - x) = 46$ Solving, we have $x = 14$. Thus, the number of oranges bought is 14.</p>	<p>1A+1A</p> <p>1M</p> <p>1A</p>	<p>pp-1 for any undefined symbol</p> <p>for leaving x or y only</p>
<p>Let x and y be the number of oranges and the number of apples bought respectively. Then, we have</p> $\begin{cases} x + y = 20 \\ 2x + 3y = 46 \end{cases}$ <p>Then, we have $2x + 3(20 - x) = 46$. Solving, we have $x = 14$. Thus, the number of oranges bought is 14.</p>	<p>------(4)</p>	<p>pp-1 for any undefined symbol</p>

Solution	Marks	Remarks
8. (a) The required probability $= \frac{5}{9}$	1A	r.t. 0.556
(b) The required probability $= 1 - \left(\frac{5}{9}\right)^2$ $= \frac{56}{81}$	1M+1M+1A 1A	1M for $1-p$ where $0 < p < 1$ + 1M for $p = \left(\frac{5}{9}\right)^2$ r.t. 0.691
The required probability $= \left(1 - \frac{5}{9}\right)\left(\frac{5}{9}\right) + \left(\frac{5}{9}\right)\left(1 - \frac{5}{9}\right) + \left(1 - \frac{5}{9}\right)\left(1 - \frac{5}{9}\right)$ $= \left(\frac{4}{9}\right)\left(\frac{5}{9}\right) + \left(\frac{5}{9}\right)\left(\frac{4}{9}\right) + \left(\frac{4}{9}\right)\left(\frac{4}{9}\right)$ $= \frac{56}{81}$	1M+1M+1A 1A	r.t. 0.691
The required probability $= \left(1 - \frac{5}{9}\right)(1) + \left(1 - \frac{5}{9}\right)\left(\frac{5}{9}\right)$ $= \frac{4}{9} + \left(\frac{4}{9}\right)\left(\frac{5}{9}\right)$ $= \frac{56}{81}$	1M+1M+1A 1A	r.t. 0.691
	------(5)	
9. (a) Let r cm be the radius of the sector. Then, we have $(\pi r^2)\left(\frac{80}{360}\right) = 162\pi$ $r = 27$ Thus, the radius of the sector is 27 cm.	1M+1A 1A	pp-1 for any undefined symbol 1M for $\frac{80}{360}$ u-1 for missing unit
Let r cm be the radius of the sector. Then, we have $\left(\frac{1}{2}r^2\right)\left(\frac{80\pi}{180}\right) = 162\pi$ $r = 27$ Thus, the radius of the sector is 27 cm.	1M+1A 1A	pp-1 for any undefined symbol 1M for $\frac{80\pi}{180}$ u-1 for missing unit
(b) The perimeter of the sector $= ((2)(27))(\pi)\left(\frac{80}{360}\right) + (2)(27)$ $= (12\pi + 54)$ cm	1M 1A	for $((2)(a))(\pi)\left(\frac{80}{360}\right) + (2)(a)$ u-1 for missing unit
The perimeter of the sector $= (27)\left(\frac{80\pi}{180}\right) + (2)(27)$ $= (12\pi + 54)$ cm	1M 1A	for $(a)\left(\frac{80\pi}{180}\right) + (2)(a)$ u-1 for missing unit
The perimeter of the sector $= \frac{2(162\pi)}{27} + (2)(27)$ $= (12\pi + 54)$ cm	1M 1A	for $\frac{2(162\pi)}{(a)} + (2)(a)$ u-1 for missing unit
	------(5)	

Solution	Marks	Remarks
<p>10. (a) Let $y = ax^2 + bx$, where a and b are non-zero constants.</p> <p>When $x = 3$, $y = 3$, so we have $9a + 3b = 3$ $3a + b = 1$ (1)</p> <p>When $x = 4$, $y = 12$, so we have $16a + 4b = 12$ $4a + b = 3$ (2)</p> <p>Solving (1) and (2), we have $\begin{cases} a = 2 \\ b = -5 \end{cases}$</p> <p>$\therefore y = 2x^2 - 5x$</p>	<p>1A</p> <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (4)</p>	<p>pp-1 for writing $y \propto ax^2 + bx$</p> <p>for substitution (either)</p> <p>for solving</p> <p>for both correct</p>
<p>(b) When $y < 42$, we have $2x^2 - 5x < 42$ (by (a)) Therefore, we have $2x^2 - 5x - 42 < 0$ $(2x + 7)(x - 6) < 0$ $\frac{-7}{2} < x < 6$</p> <p>Since x is an integer, we have $x = -3, -2, -1, 0, 1, 2, 3, 4$ or 5. Thus, all the possible values of x are $-3, -2, -1, 0, 1, 2, 3, 4$ and 5.</p>	<p>1M</p> <p>1A</p> <p>1M</p> <p>1A</p> <p>----- (4)</p>	<p>for factorization or finding roots</p>

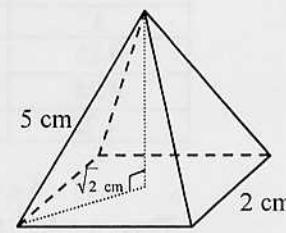
Solution	Marks	Remarks
<p>11. (a) The standard score of Paper I</p> $= \frac{54 - 46.1}{15.2}$ $= \frac{7.9}{15.2}$ ≈ 0.519736842 ≈ 0.520 <p>The standard score of Paper II</p> $= \frac{66 - 60.3}{11.6}$ $= \frac{5.7}{11.6}$ ≈ 0.49137931 ≈ 0.491 <p>\therefore the standard score of Paper II < the standard score of Paper I \therefore John did not perform better in Paper II than in Paper I.</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>1M</p> <p>----- (4)</p>	<p>either one</p> <p>r.t. 0.52</p> <p>r.t. 0.49</p>
<p>(b) After the mark adjustment,</p> <p>the new mean = 50.1 marks ,</p> <p>the new median = 50 marks ,</p> <p>the new range = 91 marks .</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>----- (3)</p>	<p>u-1 for missing unit</p> <p>u-1 for missing unit</p> <p>u-1 for missing unit</p>

Solution	Marks	Remarks
12. (a) (i) $\because CD = CE$ $\therefore \angle CED = \angle CDE = 36^\circ$ So, we have $\angle AEF = \angle CED = 36^\circ$	1A	u-1 for missing unit
(ii) $\angle ACB = \angle CDE + \angle CED = 36^\circ + 36^\circ = 72^\circ$ $\therefore AB = AC$ $\therefore \angle ABC = \angle ACB = 72^\circ$ $\therefore \angle BAC = 180^\circ - 72^\circ - 72^\circ$ $\therefore \angle BAC = 36^\circ$	1M 1A	u-1 for missing unit
-----(3)		
(b) (i) In $\triangle AEF$, $\angle BFE = 36^\circ + 36^\circ = 72^\circ$ (ext. \angle of \triangle) $\therefore \angle AEF = 36^\circ = \angle EAF$ $\therefore AF = EF$ (base \angle s equal) $\therefore AF = FB$ $\therefore EF = FB$ $\angle FEB + \angle FBE + 72^\circ = 180^\circ$ (\angle sum of \triangle) $\angle FEB = \angle FBE = \frac{180^\circ - 72^\circ}{2} = 54^\circ$ (base \angle s, isos. \triangle) $\angle AEB = 54^\circ + 36^\circ = 90^\circ$ Thus, $\angle AEB$ is a right angle.		[\triangle 的外角] [底角相等] [等角對邊相等] [等角對等邊] [等腰 \triangle 底角(等)的逆理] [\triangle 內角和] [等腰 \triangle 底角] pp-1 for missing unit
Marking Scheme :		
Case 1 Any correct proof with correct reasons.	3	
Case 2 Any correct proof without reasons.	2	
Case 3 Incomplete proof with any one correct step and correct reason.	1	
(ii) $\cos 36^\circ = \frac{10}{AB}$ $AB = \frac{10}{\cos 36^\circ}$ $AB \approx 12.36067977$ The required area $= \frac{1}{2}(AB)(AC) \sin 36^\circ$ $= \frac{1}{2}\left(\frac{10}{\cos 36^\circ}\right)^2 \sin 36^\circ$ ($\because AC = AB$) $\approx \frac{1}{2}(12.36067977)^2 \sin 36^\circ$ ≈ 44.9027966 $\approx 44.9 \text{ cm}^2$	1M	
$\tan 36^\circ = \frac{BE}{10}$ and $\cos 36^\circ = \frac{10}{AB}$ $BE \approx 7.26542528$ and $AB \approx 12.36067977$ The required area $= \frac{1}{2}(AC)(BE)$ $= \frac{1}{2}\left(\frac{10}{\cos 36^\circ}\right)(10 \tan 36^\circ)$ ($\because AC = AB$) $\approx \frac{1}{2}(12.36067977)(7.26542528)$ ≈ 44.90279764 $\approx 44.9 \text{ cm}^2$	1M	either
	1A	u-1 for missing unit
-----(6)		

Solution	Marks	Remarks
<p>13. (a) (i) Let the coordinates of E be (x, y). Then, we have</p> $\begin{cases} x = \frac{2+8}{2} = 5 \\ y = \frac{9+1}{2} = 5 \end{cases}$ <p>So, the coordinates of E are $(5, 5)$.</p> <p>(ii) $\because ABCD$ is a rhombus. $\therefore BD \perp AC$</p> <p>The slope of $AC = \frac{9-1}{2-8} = \frac{-4}{3}$</p> <p>The slope of $BD = \frac{-1}{\frac{-4}{3}} = \frac{3}{4}$</p> <p>The equation of BD is</p> $y-5 = \frac{3}{4}(x-5)$ $3x-4y+5=0$	<p>1A</p> <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (4)</p>	<p>pp-1 for missing '(' or ')'</p> <p>for point-slope form</p> <p>or equivalent</p>
<p>(b) (i) The slope of BC = the slope of AD $= \frac{-1}{7}$</p> <p>The equation of BC is</p> $y-1 = \frac{-1}{7}(x-8)$ $x+7y-15=0$	<p>1M</p> <p>1A</p>	<p>or equivalent</p>
<p>$\because BC \parallel AD$ \therefore let the equation of BC be $x+7y+c=0$, where c is a constant. Since $C(8, 1)$ lies on $x+7y+c=0$, we have</p> $8+7(1)+c=0$ $c=-15$ <p>Thus, the equation of BC is $x+7y-15=0$.</p>	<p>1M</p> <p>1A</p>	
<p>(ii) Let the coordinates of B be (h, k). Then, we have</p> $\begin{cases} 3h-4k+5=0 \\ h+7k-15=0 \end{cases}$ <p>Therefore, we have $h=1$ and $k=2$. Thus, the coordinates of B are $(1, 2)$. The length of AB</p> $= \sqrt{(2-1)^2 + (9-2)^2}$ $= \sqrt{50}$ $= 5\sqrt{2} \text{ units}$	<p>1A</p> <p>1M</p> <p>1A</p>	<p>for both correct</p> <p>for distance formula</p> <p>r.t. 7.07</p>

Solution	Marks	Remarks
<p>Let the coordinates of D be (h, k). Then, we have</p> $\begin{cases} 3h - 4k + 5 = 0 \\ h + 7k - 65 = 0 \end{cases}$ <p>Therefore, we have $h = 9$ and $k = 8$. Thus, the coordinates of D are $(9, 8)$. The length of AB = the length of DC = $\sqrt{(9-8)^2 + (8-1)^2}$ = $\sqrt{50}$ = $5\sqrt{2}$ units</p>	<p>1A 1M 1A</p>	<p>for both correct for distance formula r.t. 7.07</p>
----- (5)		

Solution	Marks	Remarks																								
<p>14. (a) Let r cm be the radius of the base of the cylinder.</p> $(2r)^2 + h^2 = ((12)(2))^2$ $4r^2 + h^2 = 576$ $r^2 = 144 - \frac{h^2}{4}$ $V = \pi r^2 h$ $V = \pi(144 - \frac{h^2}{4})h$ $V = 144\pi h - \frac{\pi}{4}h^3$	1A	pp-1 for any undefined symbol or equivalent																								
	1M	with r^2 substituted																								
	1																									
	(3)																									
<p>(b) (i) $600\pi = 144\pi h - \frac{\pi}{4}h^3$</p> $h^3 - 576h + 2400 = 0$ <p>Let $f(h) = h^3 - 576h + 2400$</p> $\therefore f(4) = 160 > 0 \text{ and } f(5) = -355 < 0$ $\therefore \text{a value of } h \text{ lies between } 4 \text{ and } 5.$	1	accept omitting the conclusion																								
<p>(ii)</p> <table border="1"> <thead> <tr> <th>a ($f(a) > 0$)</th> <th>b ($f(b) < 0$)</th> <th>$m = \frac{a+b}{2}$</th> <th>$f(m)$</th> </tr> </thead> <tbody> <tr> <td>4</td> <td>5</td> <td>4.5</td> <td>-101</td> </tr> <tr> <td>4</td> <td>4.5</td> <td>4.25</td> <td>+28.8</td> </tr> <tr> <td>4.25</td> <td>4.5</td> <td>4.375</td> <td>-36.3</td> </tr> <tr> <td>4.25</td> <td>4.375</td> <td>4.3125</td> <td>-3.80</td> </tr> <tr> <td>4.25</td> <td>4.3125</td> <td></td> <td></td> </tr> </tbody> </table> <p>$\therefore 4.25 < h < 4.3125$</p> <p>Thus, $h \approx 4.3$ (correct to 1 decimal place)</p>	a ($f(a) > 0$)	b ($f(b) < 0$)	$m = \frac{a+b}{2}$	$f(m)$	4	5	4.5	-101	4	4.5	4.25	+28.8	4.25	4.5	4.375	-36.3	4.25	4.375	4.3125	-3.80	4.25	4.3125			1M 1M	for testing sign of $f(m)$ for choosing the correct interval
a ($f(a) > 0$)	b ($f(b) < 0$)	$m = \frac{a+b}{2}$	$f(m)$																							
4	5	4.5	-101																							
4	4.5	4.25	+28.8																							
4.25	4.5	4.375	-36.3																							
4.25	4.375	4.3125	-3.80																							
4.25	4.3125																									
	1A	f.t.																								
	(4)																									
<p>(c) $286\pi = 144\pi h - \frac{\pi}{4}h^3$</p> $h^3 - 576h + 1144 = 0$ <p>Let $g(h) = h^3 - 576h + 1144$</p> $\therefore g(2) = (2)^3 - 576(2) + 1144 = 0$ <p>$\therefore 2$ is a root of $h^3 - 576h + 1144 = 0$.</p> <p>Therefore, we have $(h-2)(h^2 + 2h - 572) = 0$.</p> <p>So, we have $h = 2$ or $h = \sqrt{573} - 1$ or $h = -\sqrt{573} - 1$ (rejected).</p> <p>Thus, the height of the cylinder is 2 cm or $(\sqrt{573} - 1)$ cm.</p>	1M	for attempting to find a root by substitution																								
	1M+1A	1M for $(h-2)(ah^2 + bh + c) = 0$																								
	1A	for both correct																								
		u-1 for missing unit																								
	(4)																									

Solution	Marks	Remarks
<p>15. (a) (i) The perimeter of F_{10} $= 8 + (10 - 1)(4)$ $= 44$ cm</p> <p>(ii) $\frac{n}{2}(2(8) + (n-1)(4)) \leq 1000$ $n^2 + 3n - 500 \leq 0$ $-23.91093483 \leq n \leq 20.91093483$ Thus, the required number of distinct square frames is 20.</p>	<p>1A 1A 1A 1M 1A -----(5)</p>	<p>u-1 for missing unit for correct sum of AP pp-1 for any undefined symbol</p>
<p>(b) Let V_1 cm³, V_2 cm³ and V_3 cm³ be the volumes of S_1, S_2 and S_3 respectively.</p> <p>(i) Note that the perimeters of F_2 and F_3 are 12 cm and 16 cm respectively. So, we have $\frac{V_1}{V_2} = \left(\frac{8}{12}\right)^3 = \left(\frac{2}{3}\right)^3$ and $\frac{V_2}{V_3} = \left(\frac{12}{16}\right)^3 = \left(\frac{3}{4}\right)^3$ $\frac{V_1}{V_2} = \frac{8}{27}$ and $\frac{V_2}{V_3} = \frac{27}{64}$ $\frac{V_1}{V_2} \neq \frac{V_2}{V_3}$ Thus, the volumes of S_1, S_2, S_3 do not form a geometric sequence.</p>	<p>1A 1M</p>	<p>for either one ft.</p>
<p>(ii) The length of each side of the base of $S_1 = \frac{8}{4} = 2$ cm The length of each diagonal of the base of $S_1 = \sqrt{2^2 + 2^2} = 2\sqrt{2}$ cm The height of $S_1 = \sqrt{5^2 - (\sqrt{2})^2} = \sqrt{23}$ cm $V_1 = \frac{1}{3}(2)^2\sqrt{23}$ $V_1 = \frac{4}{3}\sqrt{23}$ $\frac{V_3}{V_1} = \left(\frac{16}{8}\right)^3 = 8$ $V_3 = 8\left(\frac{4}{3}\sqrt{23}\right) = \frac{32}{3}\sqrt{23}$ Thus, the volumes of S_3 is $\frac{32}{3}\sqrt{23}$ cm³.</p>	<p>1M 1M 1A 1A</p>	<p></p> <p>can be absorbed u-1 for missing unit</p>
<p>The length of each slant edge of $S_3 = 5\left(\frac{16}{8}\right) = 10$ cm The length of each side of the base of $S_3 = \frac{16}{4} = 4$ cm The length of each diagonal of the base of $S_3 = \sqrt{4^2 + 4^2} = 4\sqrt{2}$ cm The height of $S_3 = \sqrt{10^2 - (2\sqrt{2})^2} = 2\sqrt{23}$ cm $V_3 = \frac{1}{3}(16)(2\sqrt{23}) = \frac{32}{3}\sqrt{23}$ Thus, the volumes of S_3 is $\frac{32}{3}\sqrt{23}$ cm³.</p>	<p>1A 1M 1M+1A</p>	<p>can be absorbed u-1 for missing unit</p>
	<p>-----(6)</p>	

	Solution	Marks	Remarks
16.	Marking Scheme for (a) and (b) :		
	Case 1 Any correct proof with correct reasons.	3	
	Case 2 Any correct proof without reasons.	2	
	Case 3 Incomplete proof with any one correct step and one correct reason.	1	
(a)	<p>In $\triangle ADE$ and $\triangle BOE$,</p> <p>$\angle ADE = \angle DBC$ (alt. \angles, $OD \parallel BC$)</p> <p>$= \angle BOE$ (\angle in alt. segment)</p> <p>$\angle DAE = \angle OBE$ (ext. \angle, cyclic quad.)</p> <p>$AD = BO$ (given)</p> <p>$\therefore \triangle ADE \cong \triangle BOE$ (ASA)</p>	(3)	<p>[錯角, $OD \parallel BC$]</p> <p>[交錯弓形的圓周角] [弦切角定理]</p> <p>[圓內接四邊形外角]</p> <p>[已知]</p>
(b)	<p>$AE = BE$ (by (a))</p> <p>$\angle AOE = \angle BOE$ (equal chords, equal \angles)</p> <p>$\angle BEO = \angle AED$ (by (a))</p> <p>$= \angle AOB$ (ext. \angle, cyclic quad.)</p> <p>$= \angle AOE + \angle BOE$</p> <p>$= 2\angle BOE$</p>		<p>[等弦對等角]</p> <p>[圓內接四邊形外角]</p>
	<p>$DE = OE$ (by (a))</p> <p>$\angle ADE = \angle AOE$ (base \angles, isos. \triangle)</p> <p>$\angle ADE = \angle BOE$ (by (a))</p> <p>Hence, $\angle AOE = \angle BOE$</p> <p>Thus, $\angle BEO = \angle AOE + \angle ADE$ (ext. \angle of \triangle)</p> <p>$= 2\angle BOE$</p>		<p>[等腰\triangle底角]</p> <p>[\triangle的外角]</p>
(c) (i)	<p>$\therefore OE$ is a diameter of the circle $OAEB$.</p> <p>$\therefore \angle OBE = 90^\circ$</p> <p>By (b), $\angle BEO = 2\angle BOE$</p> <p>$\angle BOE + \angle BEO + \angle OBE = 180^\circ$</p> <p>$\angle BOE + 2\angle BOE + 90^\circ = 180^\circ$</p> <p>Thus, $\angle BOE = 30^\circ$</p>	1A 1A	
(ii)	<p>Note that $E = (6, 6 \tan 30^\circ) = (6, 2\sqrt{3})$. Then,</p> <p>the coordinates of the centre of the circle $OAEB$</p> <p>$= \left(\frac{6+0}{2}, \frac{2\sqrt{3}+0}{2} \right) = (3, \sqrt{3})$</p> <p>Also, the radius of the circle $OAEB = \sqrt{3^2 + (\sqrt{3})^2} = 2\sqrt{3}$</p> <p>Hence, the equation of the circle $OAEB$ is</p> <p>$(x-3)^2 + (y-\sqrt{3})^2 = (2\sqrt{3})^2$</p> <p>$x^2 + y^2 - 6x - 2\sqrt{3}y = 0$</p>	1A 1M 1A	<p>either one</p>
	<p>\therefore the circle $OAEB$ passes through the origin.</p> <p>\therefore let the equation of the circle $OAEB$ be $x^2 + y^2 + ax + by = 0$.</p> <p>\therefore the coordinates of $B = (6, 0)$</p> <p>$\therefore 6^2 + 0^2 + a(6) + b(0) = 0$</p> <p>So, we have $a = -6$.</p> <p>\therefore the coordinates of $E = (6, 6 \tan 30^\circ) = (6, 2\sqrt{3})$</p> <p>$\therefore 6^2 + (2\sqrt{3})^2 - 6(6) + b(2\sqrt{3}) = 0$</p> <p>Therefore, we have $b = -2\sqrt{3}$.</p> <p>Thus, the equation of the circle $OAEB$ is $x^2 + y^2 - 6x - 2\sqrt{3}y = 0$.</p>	1M 1A 1A	
		(5)	

Solution	Marks	Remarks
<p>17. (a) (i) $\sin 30^\circ = \frac{FF'}{20}$ $FF' = 20 \sin 30^\circ$ $FF' = 10 \text{ m}$ $\cos 30^\circ = \frac{EF'}{20}$ $EF' = 20 \cos 30^\circ$ $EF' = 10\sqrt{3}$ $\tan 60^\circ = \frac{FF'}{AF'}$ $AF' = \frac{10}{\tan 60^\circ}$ $AF' = \frac{10\sqrt{3}}{3}$ $AE^2 = AF'^2 + EF'^2$ $AE^2 = \left(\frac{10\sqrt{3}}{3}\right)^2 + (10\sqrt{3})^2$ $AE = \frac{10\sqrt{30}}{3} \text{ m}$</p>	<p>1M 1A 1M 1A</p>	<p>----- either one u-1 for missing unit ----- $EF' \approx 17.32050808$ with FF' substituted $AF' \approx 5.773502692$ u-1 for missing unit r.t. 18.3 m, $AE \approx 18.25741858 \text{ m}$</p>
<p>(ii) $\sin 60^\circ = \frac{FF'}{AF}$ $AF = \frac{10}{\sin 60^\circ}$ $AF = \frac{20\sqrt{3}}{3}$ By cosine formula, we have $\cos \angle AEF = \frac{EF^2 + AE^2 - AF^2}{2EF \cdot AE}$ $\cos \angle AEF = \frac{20^2 + \left(\frac{10\sqrt{30}}{3}\right)^2 - \left(\frac{20\sqrt{3}}{3}\right)^2}{(2)(20)\left(\frac{10\sqrt{30}}{3}\right)}$ $\cos \angle AEF = \frac{3\sqrt{30}}{20}$ $\angle AEF \approx 34.75634244^\circ$ $\angle AEF \approx 34.8^\circ$</p>	<p>1M 1A</p>	<p>$AF \approx 11.54700538$ $\cos \angle AEF \approx \frac{20^2 + 18.25741858^2 - 11.54700538^2}{2(20)(18.25741858)}$ $\cos \angle AEF \approx 0.821583836$ u-1 for missing unit r.t. 34.8°</p>
----- (7)		

Solution	Marks	Remarks
<p>(b) Let t_{red} s and t_{yellow} s be the time required for the red toy car and the yellow toy car to reach B respectively. Then, we have $BE = 2t_{\text{red}}$ and $BF = 3t_{\text{yellow}}$ By sine formula, we have $\frac{BE}{\sin 20^\circ} \approx \frac{BF}{\sin(180^\circ - 34.75634244^\circ)}$ $\frac{2t_{\text{red}}}{\sin 20^\circ} \approx \frac{3t_{\text{yellow}}}{\sin 34.75634244^\circ}$ $\frac{t_{\text{yellow}}}{t_{\text{red}}} \approx \frac{2\sin 34.75634244^\circ}{3\sin 20^\circ}$ $\frac{t_{\text{yellow}}}{t_{\text{red}}} \approx 1.111216642$ $\frac{t_{\text{yellow}}}{t_{\text{red}}} \approx 1.11$ $\frac{t_{\text{yellow}}}{t_{\text{red}}} > 1$ Thus, $t_{\text{yellow}} > t_{\text{red}}$ So, the yellow toy car will not reach the point B before the red toy car.</p>	<p>1M 1M 1A 1A</p>	<p>for attempting to find $\frac{t_{\text{yellow}}}{t_{\text{red}}}$ $\frac{t_{\text{red}}}{t_{\text{yellow}}} \approx 0.899914528$ accept $\frac{t_{\text{red}}}{t_{\text{yellow}}} \approx 0.900$ and can be absorbed $\frac{t_{\text{red}}}{t_{\text{yellow}}} < 1$ $t_{\text{red}} < t_{\text{yellow}}$ f.t.</p>
<p>$\angle EBF \approx 34.75634244^\circ - 20^\circ \approx 14.75634244^\circ$ By sine formula, we have $\frac{BE}{\sin 20^\circ} = \frac{20}{\sin \angle EBF} \quad \text{and} \quad \frac{BF}{\sin(180^\circ - 34.75634244^\circ)} \approx \frac{20}{\sin \angle EBF}$ $BE \approx \frac{20\sin 20^\circ}{\sin 14.75634244^\circ} \quad \text{and} \quad BF \approx \frac{20\sin 34.75634244^\circ}{\sin 14.75634244^\circ}$ $BE \approx 26.85575694 \quad \text{and} \quad BF \approx 44.76384605$ Let t_{red} s and t_{yellow} s be the time required for the red toy car and the yellow toy car to reach B respectively. Then, we have $BE = 2t_{\text{red}}$ and $BF = 3t_{\text{yellow}}$ $t_{\text{red}} \approx \frac{26.85575694}{2} \quad \text{and} \quad t_{\text{yellow}} \approx \frac{44.76384605}{3}$ $t_{\text{red}} \approx 13.42787847 \quad \text{and} \quad t_{\text{yellow}} \approx 14.92128202$ $t_{\text{red}} \approx 13.4 \quad \text{and} \quad t_{\text{yellow}} \approx 14.9$ Thus, $t_{\text{yellow}} > t_{\text{red}}$ So, the yellow toy car will not reach the point B before the red toy car.</p>	<p>1M 1A 1A</p>	<p>either with $\angle EBF$ substituted for both for either (can be absorbed) f.t.</p>
	<p>------(4)</p>	